

# Understanding Language Models Through the Lens of their Training Data

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University of Toronto & Vector Institute

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*memorization*

*arithmetic*

*fact-learning*

*zero-shot generalization\**

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AI created a song mimicking the work of Drake and The Weeknd. What does that mean for copyright law?

A Harvard Law expert explains why AI-generated art doesn't qualify for copyright protection — but how it nonetheless will 'materially affect' the music industry

## ***The Times Sues OpenAI and Microsoft Over A.I. Use of Copyrighted Work***

Millions of articles from The New York Times were used to train chatbots that now compete with it, the lawsuit said.

**COPYRIGHT —**

## **Stable Diffusion copyright lawsuits could be a legal earthquake for AI**

Experts say generative AI is in uncharted legal waters.

## *What do I mean by “understanding through the lens of training data”*

1. Understanding the relationship between an LLM’s capabilities and the *quantity of relevant information* in its training set

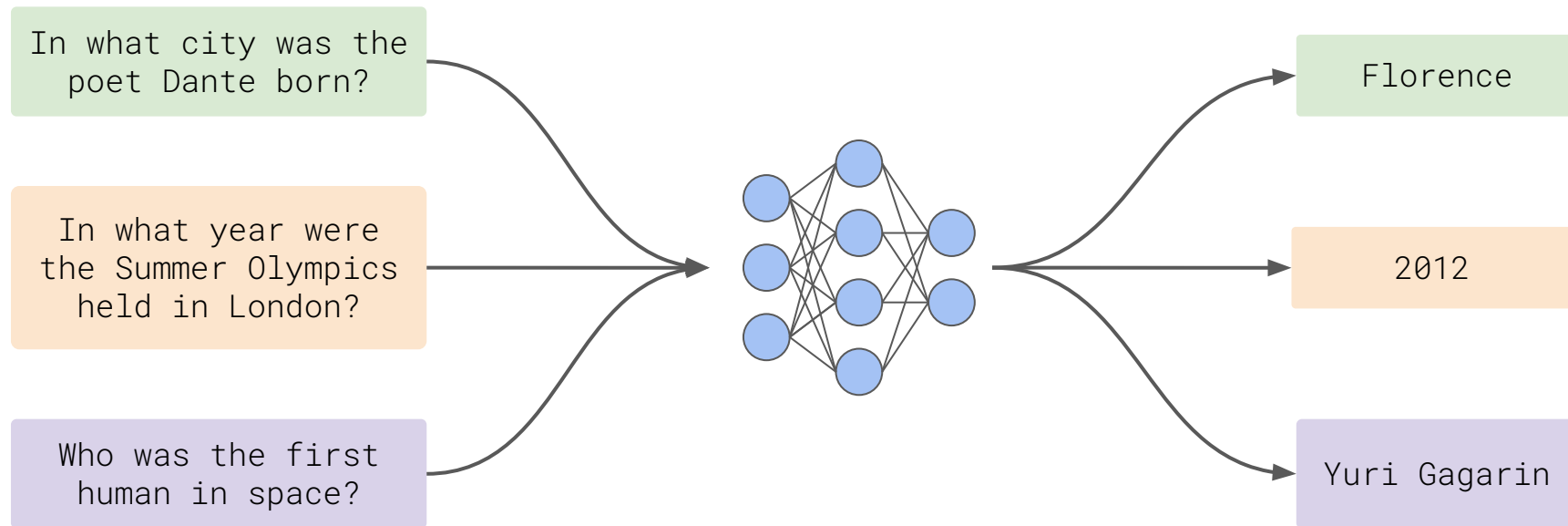
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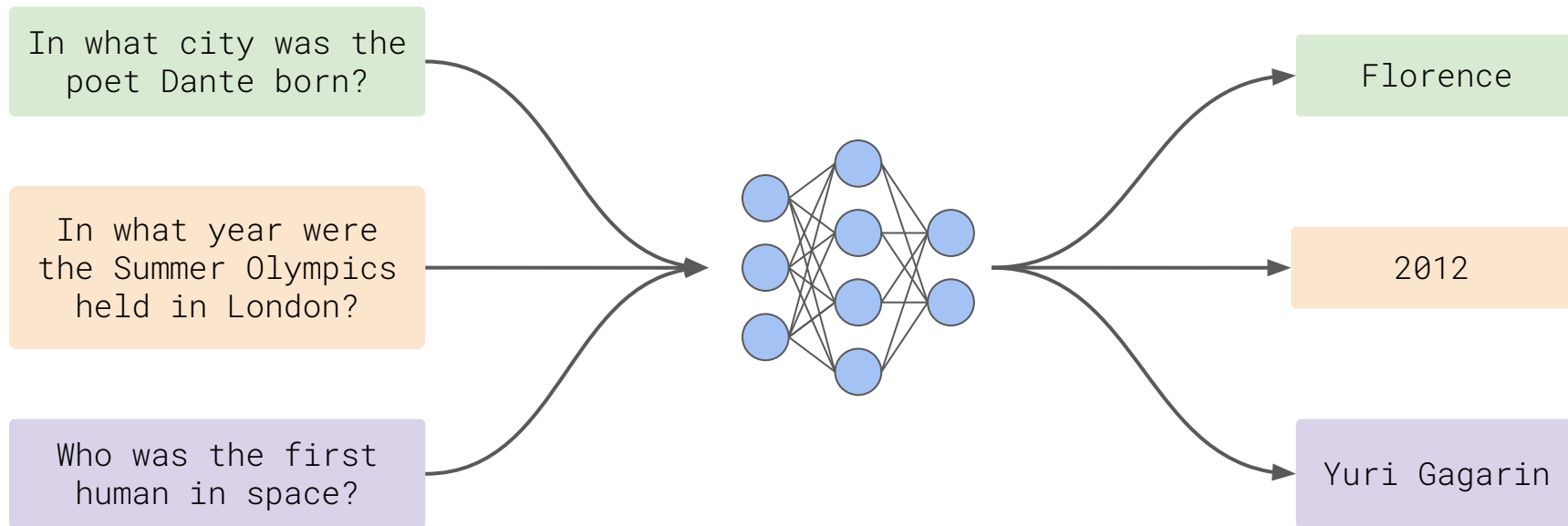
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## *Pre-trained language models capture a wide range of knowledge*



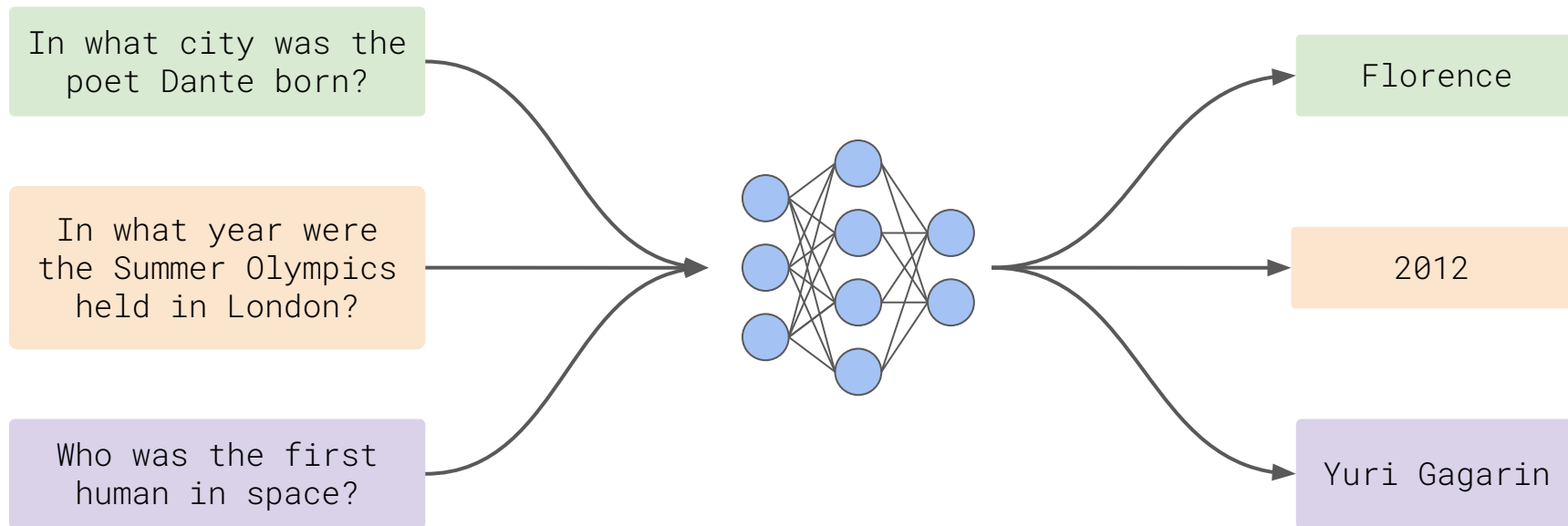
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(How) is this related to the quantity of relevant training data?

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1. Identify a set of facts
2. Count how many times each fact occurs in a pre-training dataset
3. Evaluate an LM's ability to recall each fact

*Identifying a set of facts*

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### **Question - Answer Pair**

In what city was the poet Dante born?

Florence



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**Question - Answer Pair**

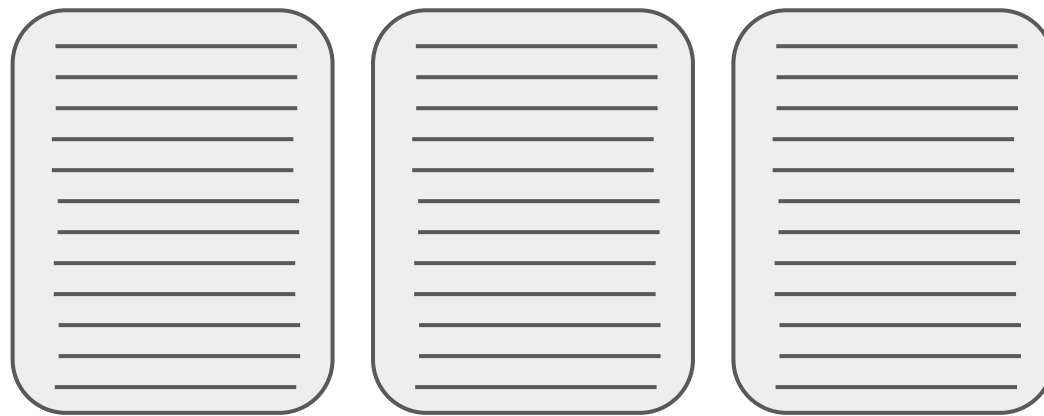
( In what city was the poet Dante born? , Florence )

**Fact**

The poet Dante was born in the city of Florence



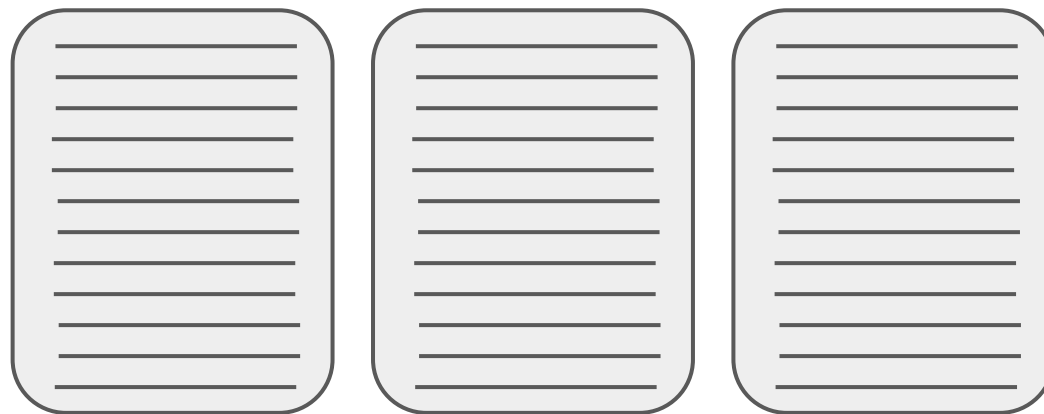
## *Counting fact instances in pre-training datasets*



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## Counting fact instances in pre-training datasets

1. Entity link Q-A pair



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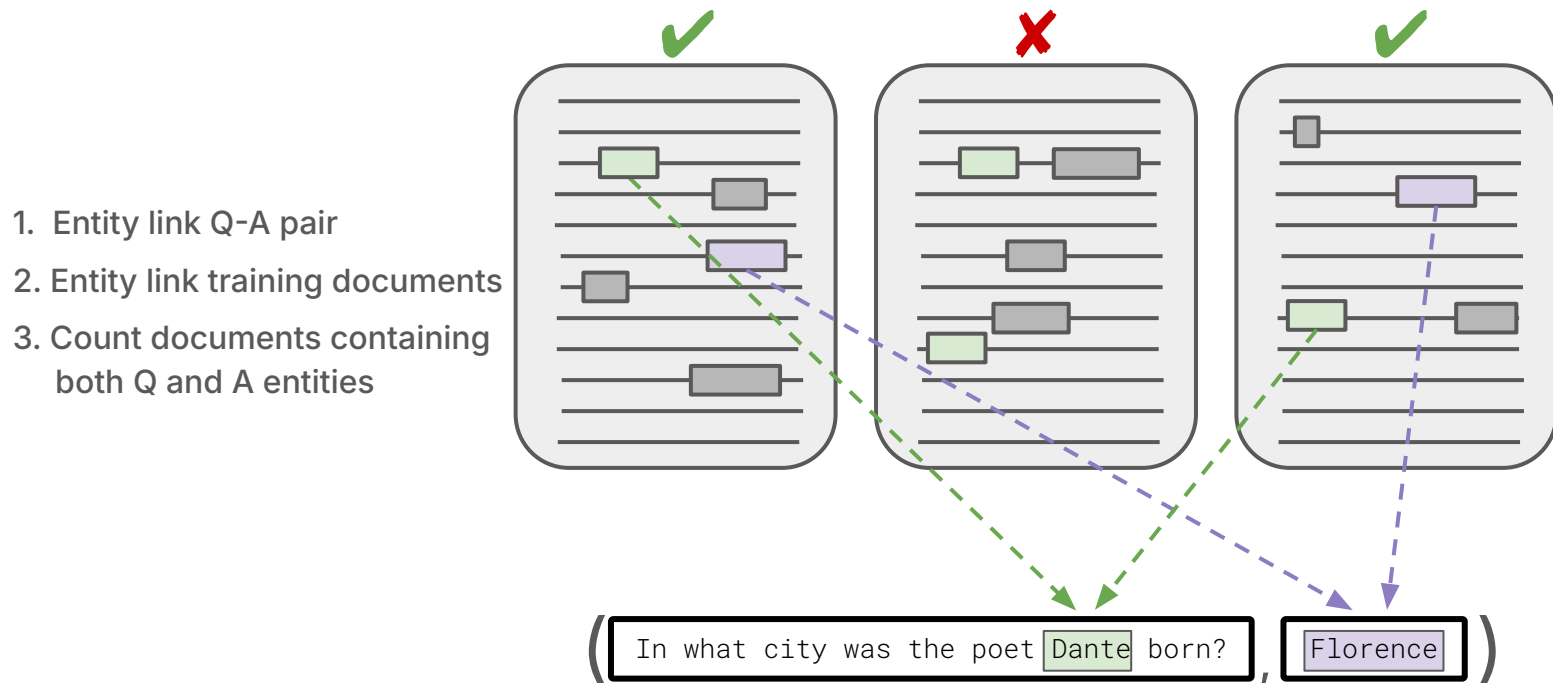
## Counting fact instances in pre-training datasets

1. Entity link Q-A pair
2. Entity link training documents



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## Counting fact instances in pre-training datasets

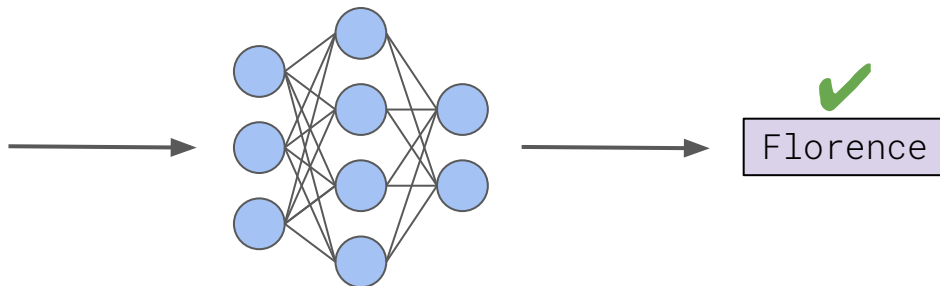


## *Evaluating a Language Model's Fact Recall*

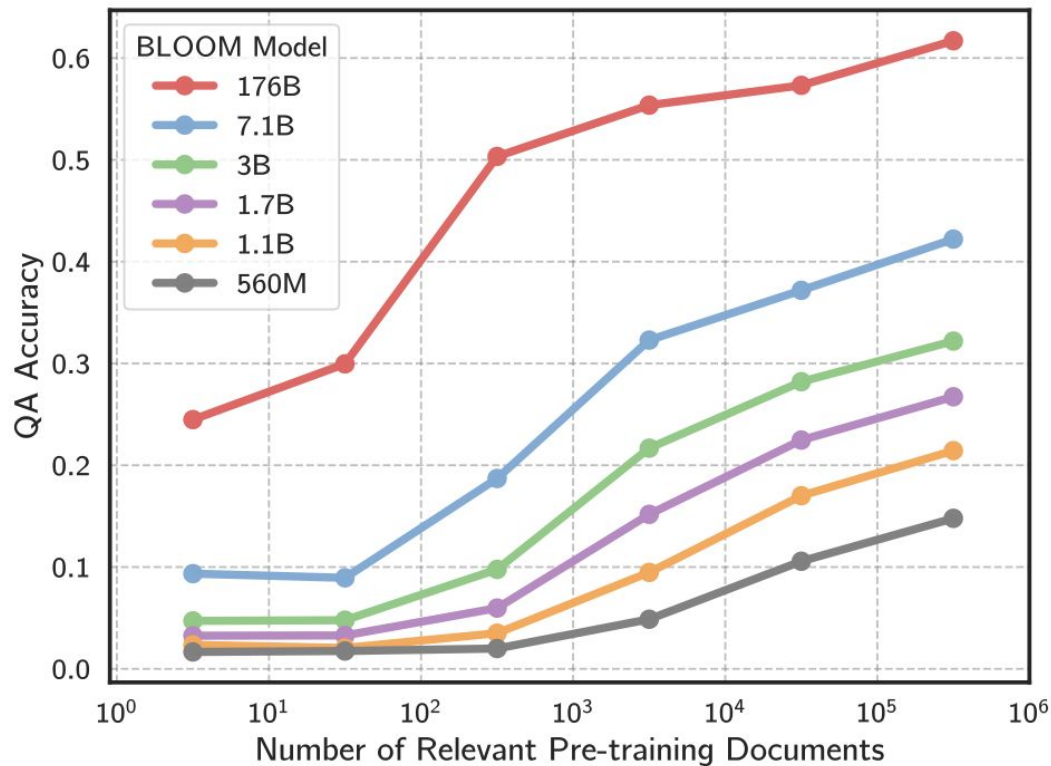
# Evaluating a Language Model's Fact Recall

## Few-Shot Question Answering

Q: In what year were the Summer Olympics held in London?
A: 2012
Q: Who was the first human in space?
A: Yuri Gagarin
Q: In what city was the poet Dante born?
A:

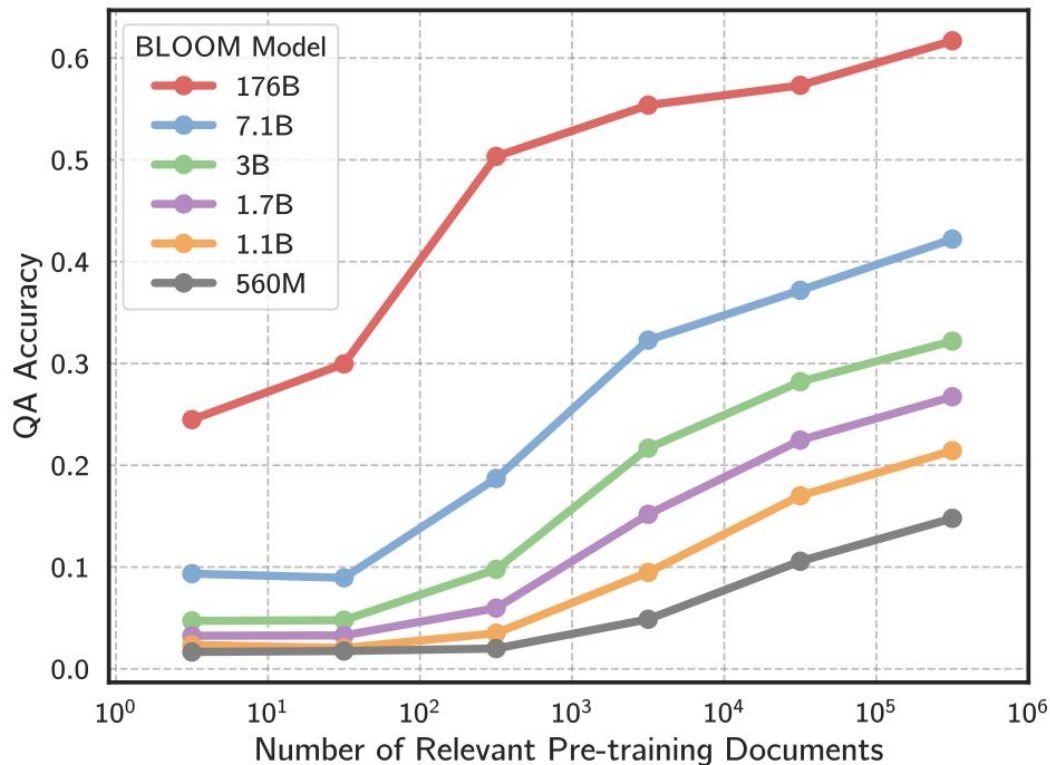


## *Language models struggle to capture long-tail facts*





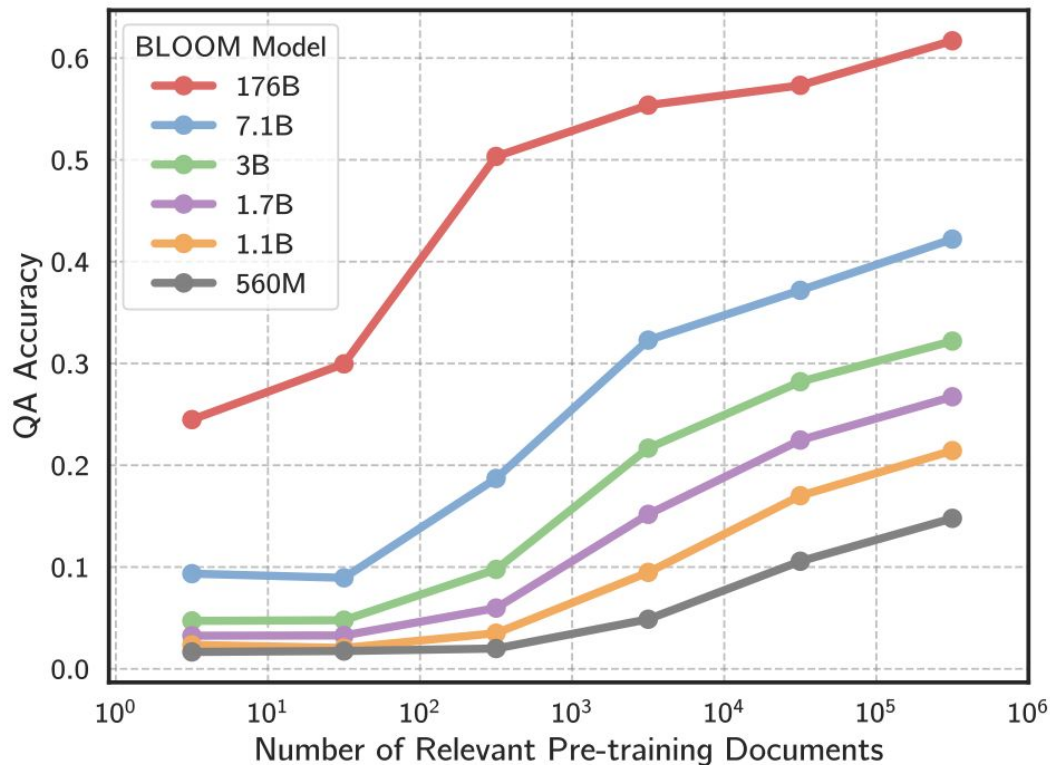
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### Observation #1

Larger models are more effective at capturing facts that are both rare and common in the training data

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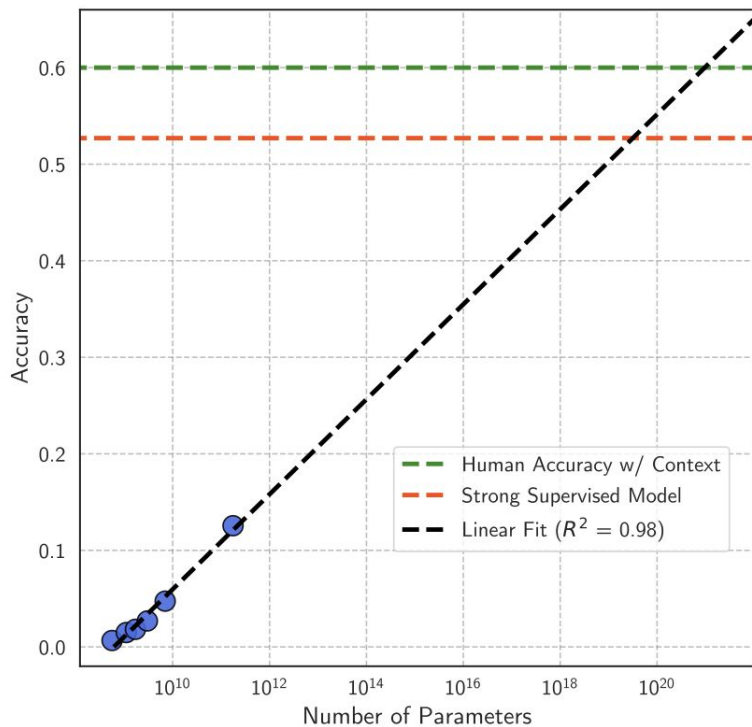
### Observation #2

Models of all sizes require a fact to be present many times in the training data to reliably learn that fact

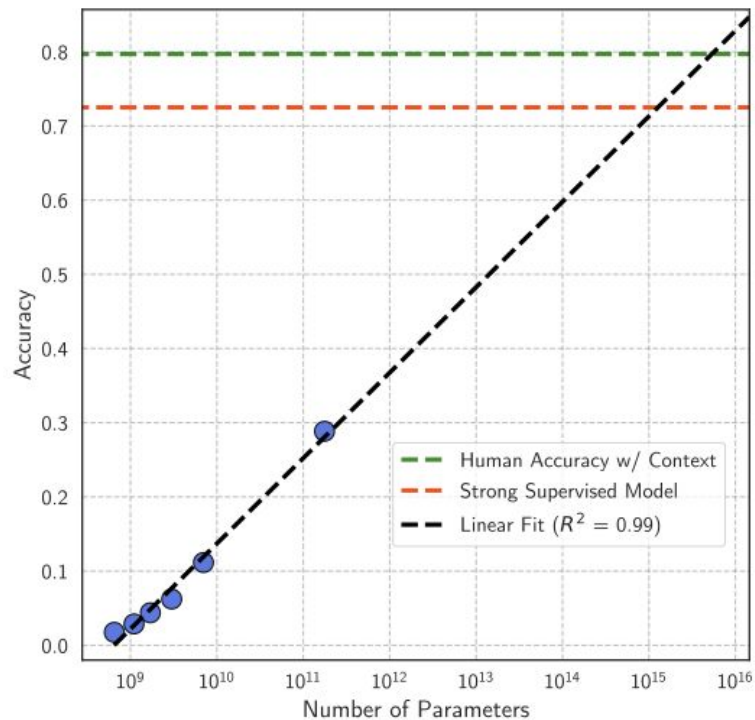
*Scaling model size has diminishing returns for learning long-tail knowledge*

# Scaling model size has diminishing returns for learning long-tail knowledge

## Natural Questions Rare Fact Accuracy



## TriviaQA Rare Fact Accuracy

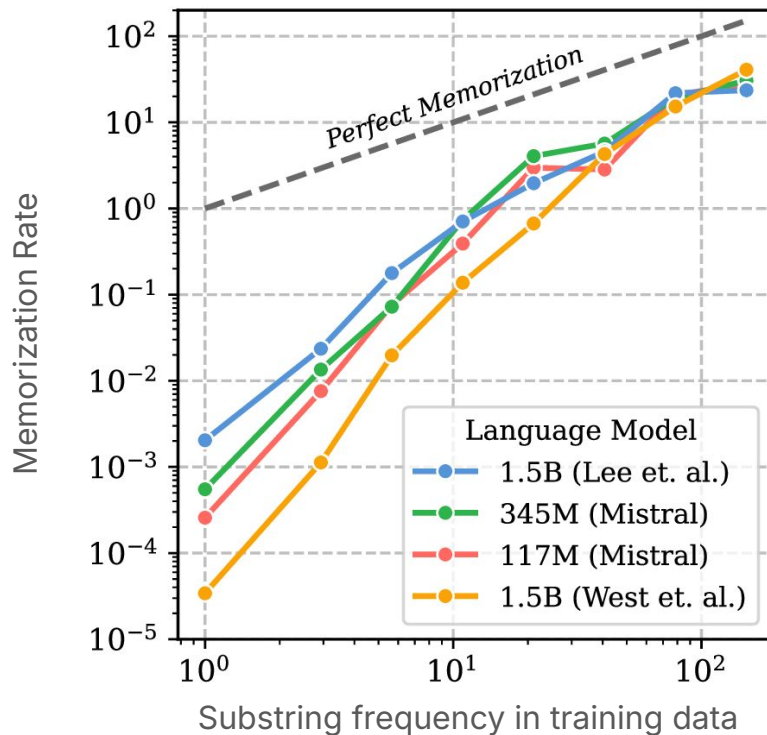


*What other capabilities have been characterized in this way?*

# Quantity of relevant data influences language model capabilities

Example 1: LMs tend to memorize text that appears more in training data

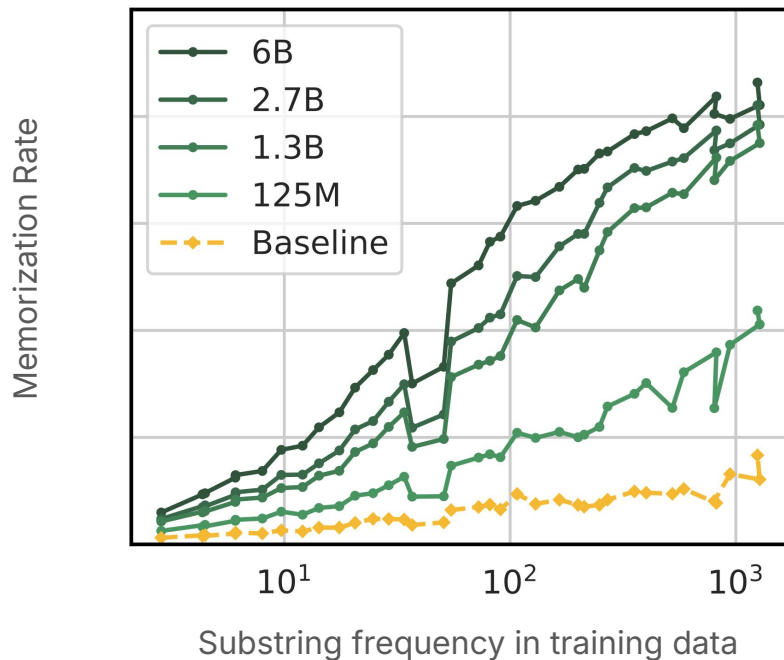
[Kandpal et. al. \(2022a\)](#)



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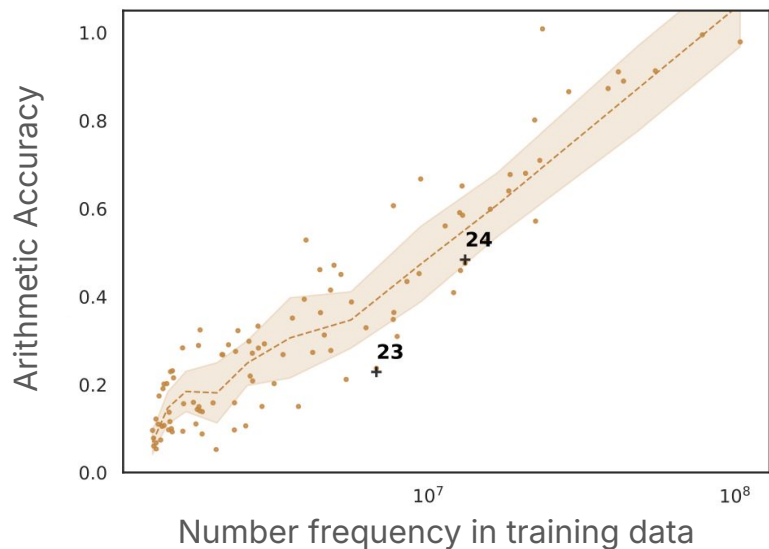
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Kandpal et. al. (2022a), Carlini et. al. (2022)

Example 2: LMs excel at arithmetic on numbers that appear more in the training data

Razeghi et. al. (2022)

Q: What is 24 times 18? A: \_\_\_\_ Model: 432 ✓  
Q: What is 23 times 18? A: \_\_\_\_ Model: 462 ✗





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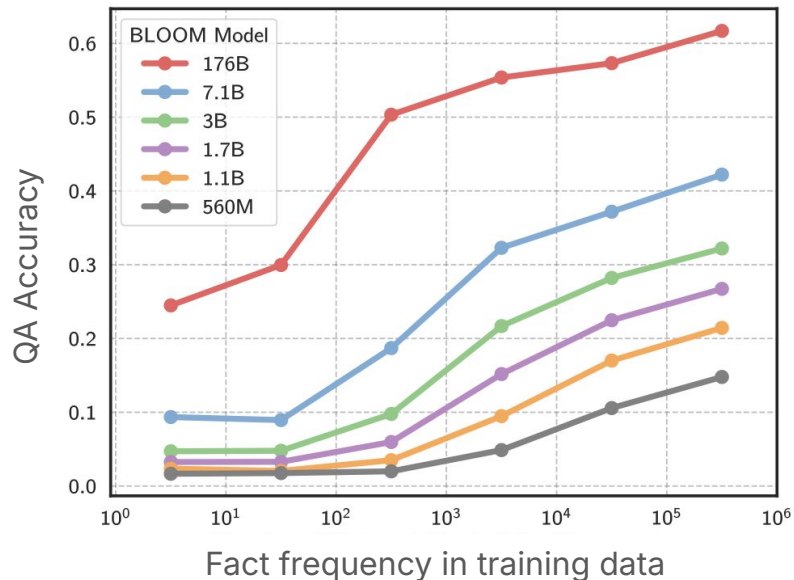
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[Kandpal et. al. \(2022b\)](#)



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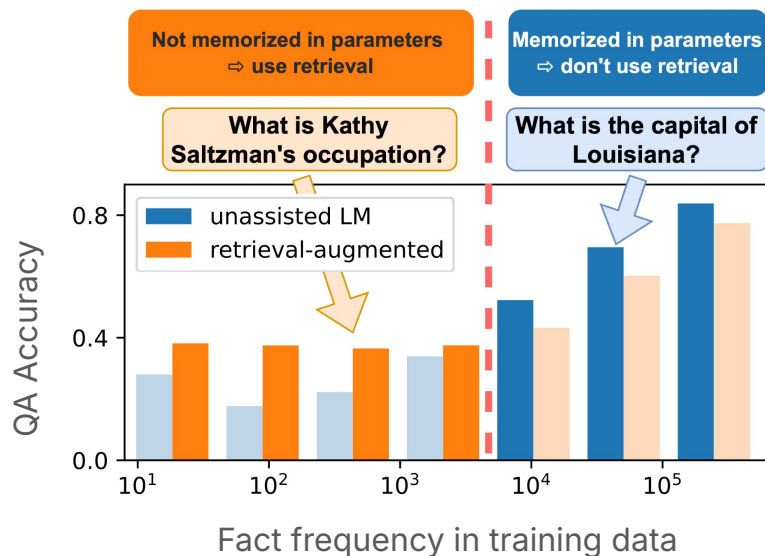
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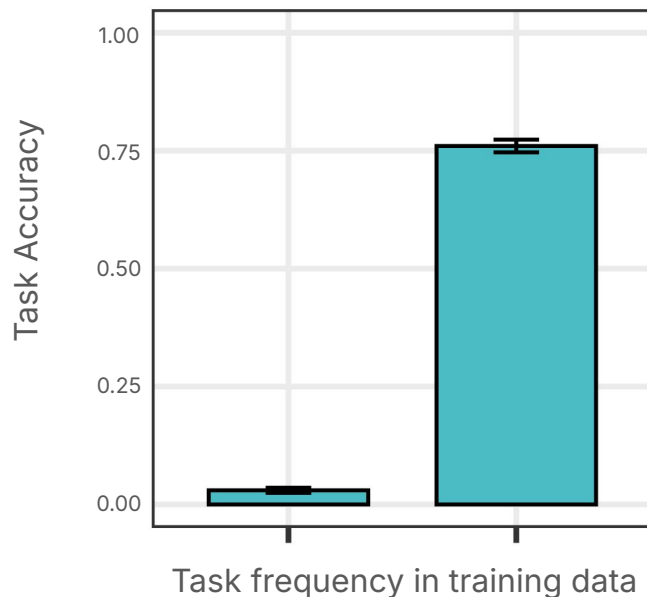
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Example 3: LMs learn facts that appear more in the training data

Kandpal et. al. (2022b), Mallen et. al. (2022)

Example 4: LMs can perform variants of a task when that variant appears more in the training data

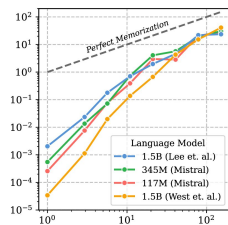
[Mccoy et. al. \(2023\)](#)



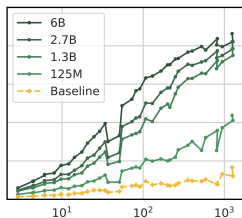
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## Memorization

Kandpal et. al. (2022a)

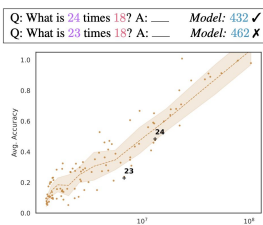


Carlini et. al. (2022)



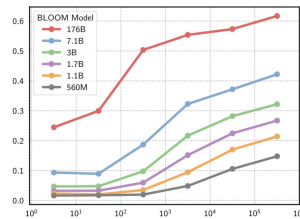
## Arithmetic

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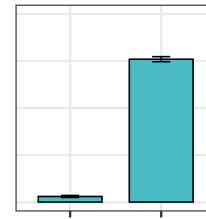
## Fact Learning

Kandpal et. al. (2022b)

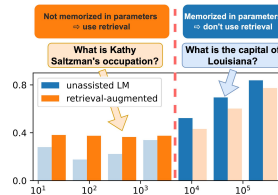


## Task Learning

Mccoy et. al. (2023)



Mallen et. al. (2022)

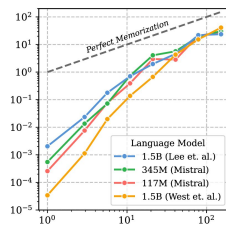


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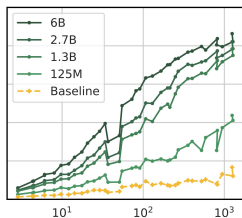
## Higher-level (more "interesting") behaviors

### Memorization

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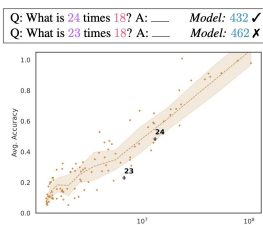


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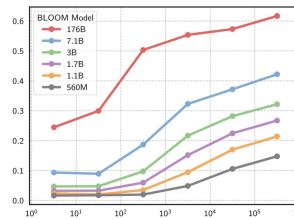
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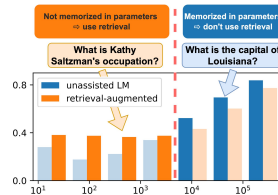


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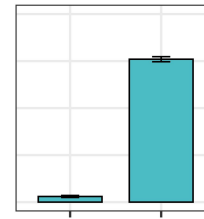


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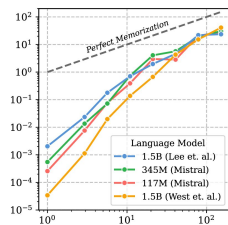
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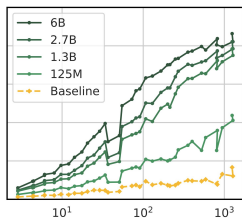
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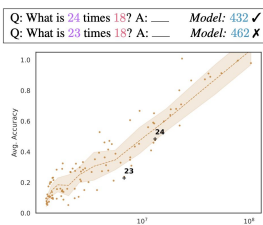


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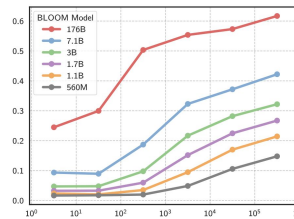
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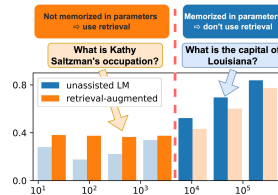


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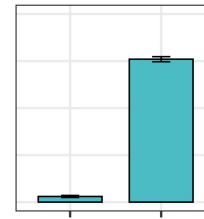


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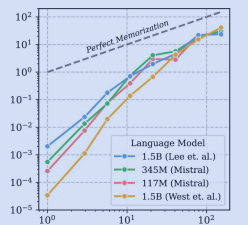
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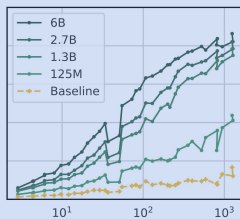
## Exactly Compute Training Frequency

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Kandpal et. al. (2022a)

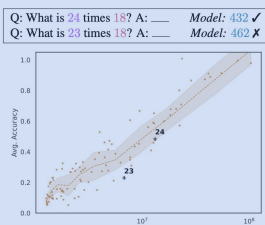


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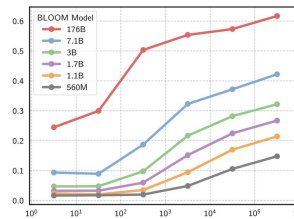
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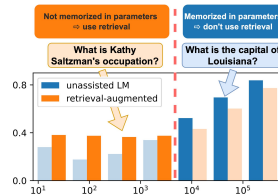


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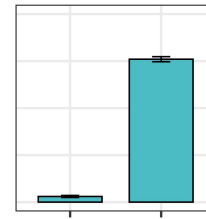


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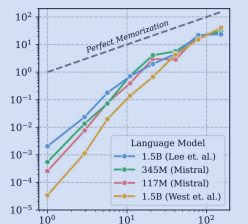
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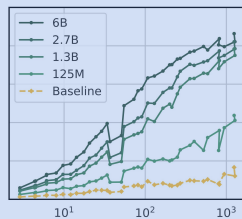
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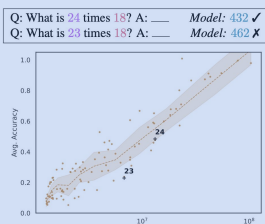


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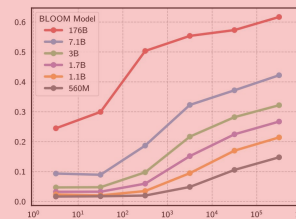
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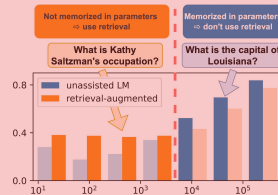
## Approximate Training Frequency

### Fact Learning

Kandpal et. al. (2022b)

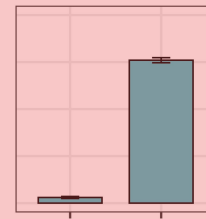


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### Task Learning

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These only accurately simulate leave-one-out retraining when...

- Models are trained with a strongly-convex objective
- Models are trained to convergence
- Training is deterministic

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Instead let's focus on methods that allow *exact(!)* and *scalable(!)* attribution under more realistic assumptions

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**Assume:** Our dataset is heterogeneous, containing some data that we *must do* attribution for and some *that do not need* attribution

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### **Coming Soon: The Common Pile**

~2 trillion tokens of permissively licensed and public domain text



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### **Approach:**

1. Pre-train an LLM on data that does not require attribution
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Semi-Parametric Language Models

Retrieval-Augmented Generation (RAG)



## *kNN-LM: One Flavor of a Semi-Parametric Language Model*

<b>Test Context</b> $x$	<b>Target</b>
<i>Obama's birthplace is</i>	?

Figure from [Khandelwal et. al. 2020](#)

## *kNN-LM: One Flavor of a Semi-Parametric Language Model*


Test Context $x$	Target	Representation $q = f(x)$
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Figure from [Khandelwal et. al. 2020](#)

# *kNN-LM: One Flavor of a Semi-Parametric Language Model*

<b>Training Contexts</b> $c_i$	<b>Targets</b> $v_i$	<b>Representations</b> $k_i = f(c_i)$
Obama was senator for	Illinois	
Barack is married to	Michelle	
Obama was born in	Hawaii	
...	...	...
Obama is a native of	Hawaii	

<b>Test Context</b> $x$	<b>Target</b>	<b>Representation</b> $q = f(x)$
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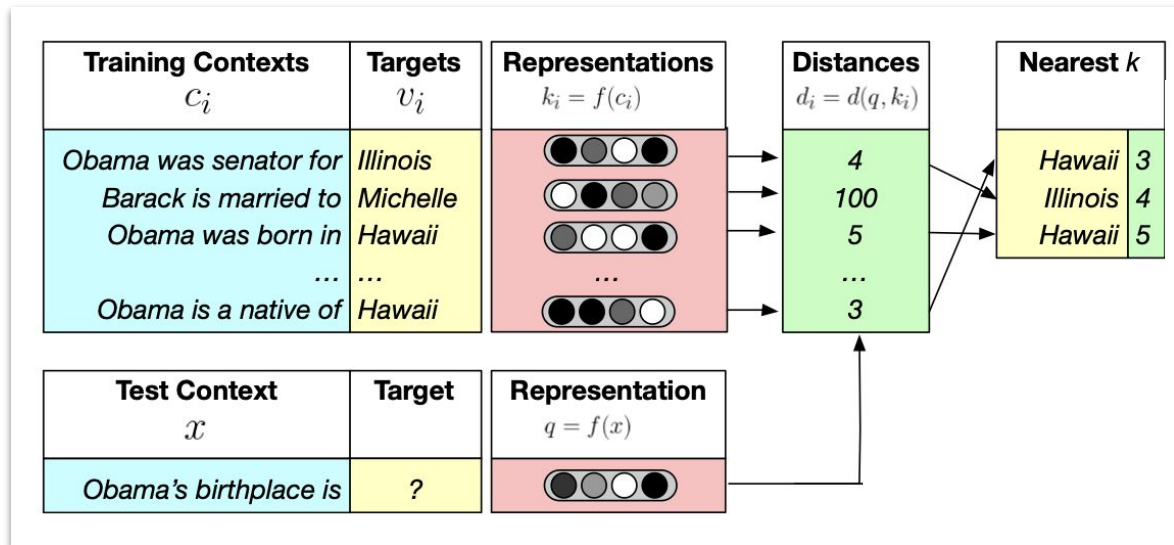


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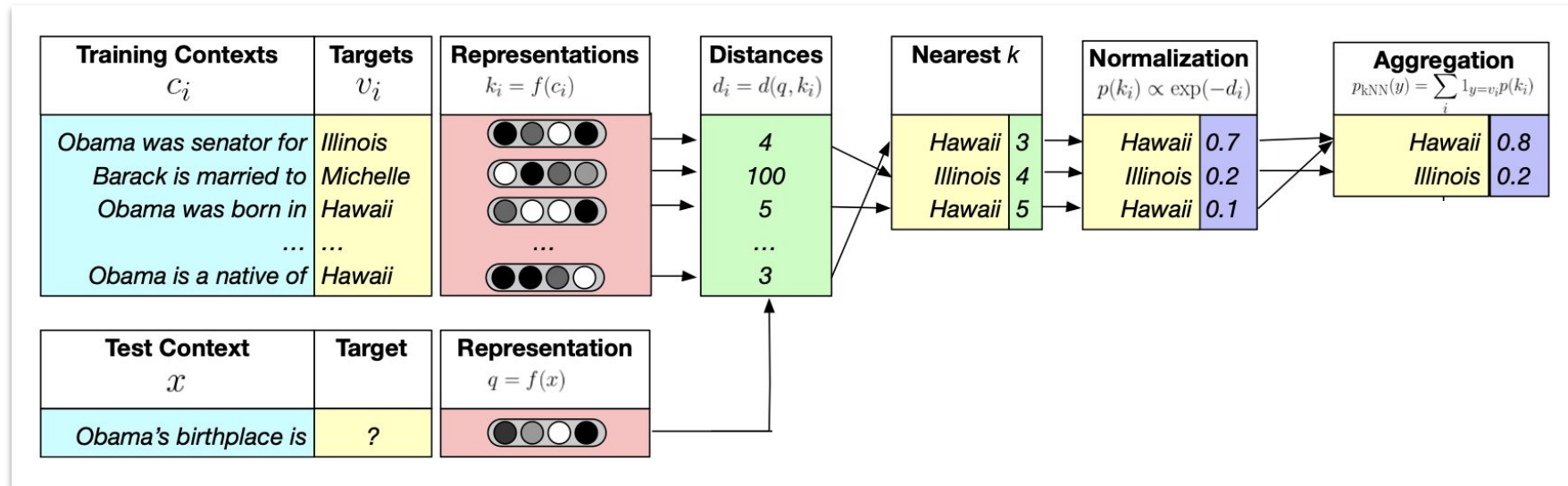


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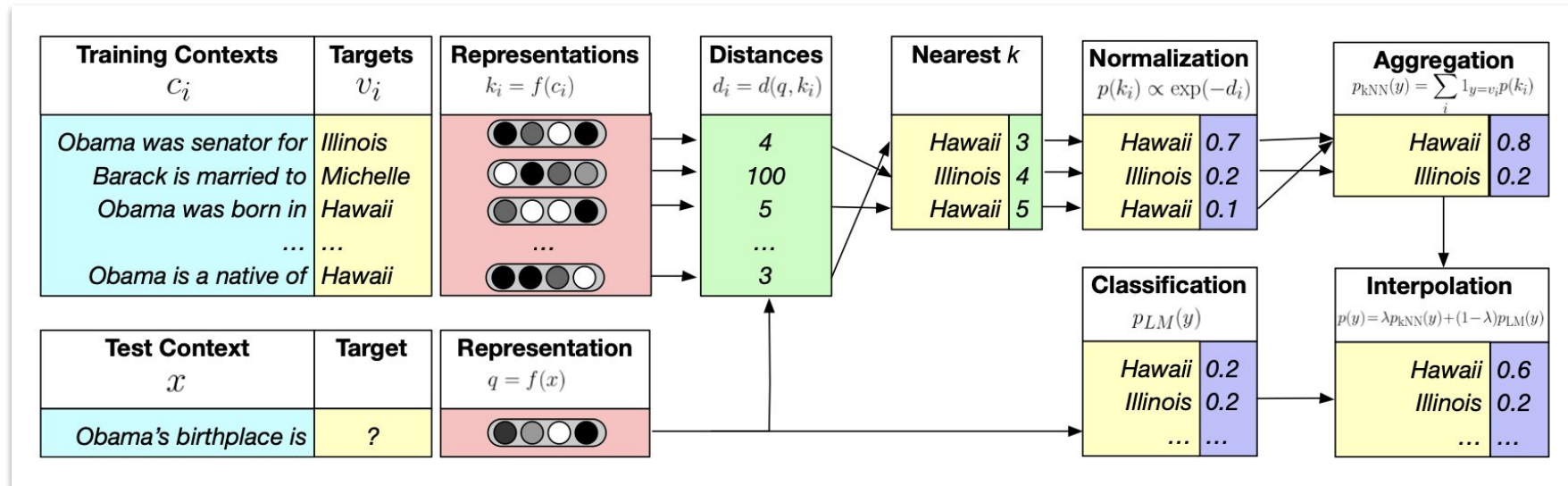


Figure from [Khandelwal et. al. 2020](#)

# kNN-LM: One Flavor of a Semi-Parametric Language Model

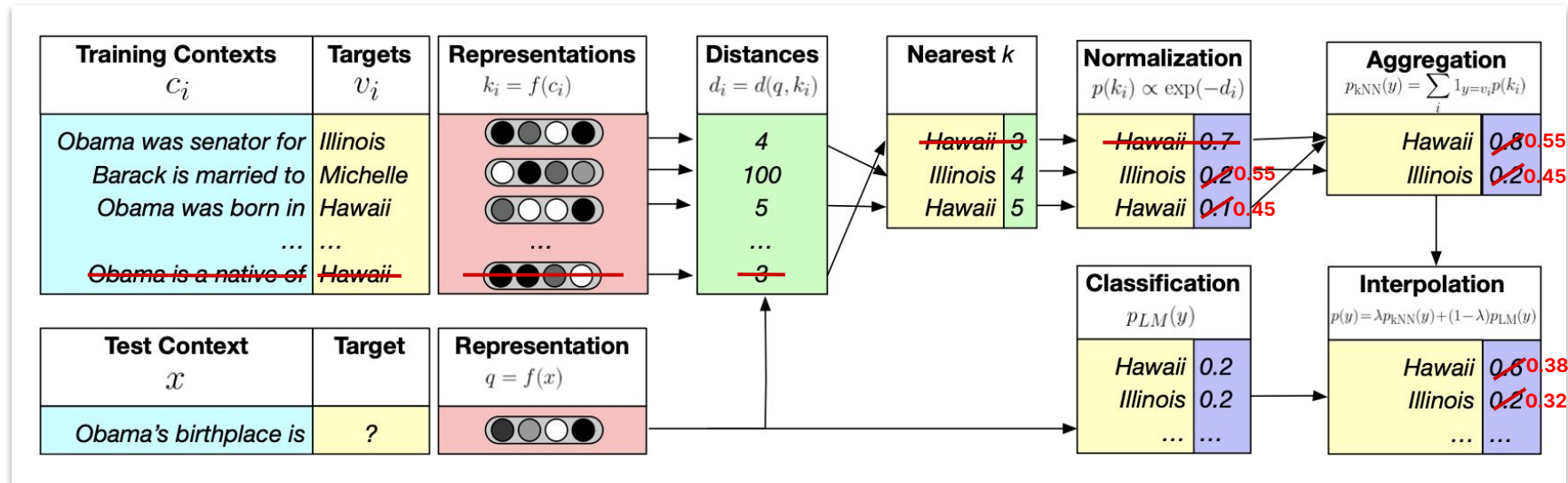
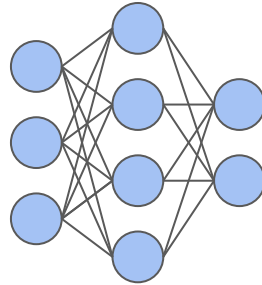


Figure from [Khandelwal et. al. 2020](#)

# *Retrieval Augmented Generation (RAG)*

Q: In what city was  
the poet Dante born?





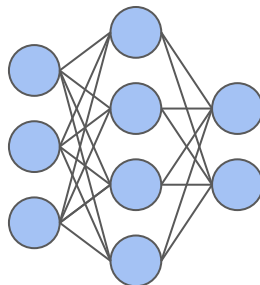
# Retrieval Augmented Generation (RAG)

Poetry is a form of literary art that uses aesthetic and rhythmic...

⋮

Dante Alighieri, commonly known as Dante, is an Italian poet, writer, ...

Q: In what city was the poet Dante born?



Florence	0.7
Rome	0.3

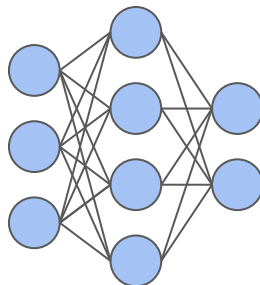
# Retrieval Augmented Generation (RAG)

Poetry is a form of literary art that uses aesthetic and rhythmic...

⋮

~~Dante Alighieri, commonly known as Dante, is an Italian poet, writer, ...~~

Q: In what city was the poet Dante born?



Florence	<del>0.7</del>	0.4
Rome	<del>0.3</del>	0.6

## *An interesting research question on incentive-alignment*

- If training data contributors were paid proportionally to the counterfactual value of their data, what kind of data are they incentivized to produce?
  - High-attribution → high-quality data?
  - High-attribution adversarial examples?

# References

## Capabilities and Relevant Training Data

1. Nikhil Kandpal, Eric Wallace, Colin Raffel. [Deduplicating Training Data Mitigates Privacy Risks in Language Models](#). 2022a.
2. Nicholas Carlini, Daphne Ippolito, Matthew Jagielski, Katherine Lee, Florian Tramèr, Chiyuan Zhang. [Quantifying Memorization Across Neural Language Models](#). 2022.
3. Yasaman Razeghi, Robert L. Logan IV, Matt Gardner, Sameer Singh. [Impact of Pretraining Term Frequencies on Few-Shot Reasoning](#). 2022.
4. Nikhil Kandpal, Haikang Deng, Adam Roberts, Eric Wallace, Colin Raffel. [Large Language Models Struggle to Learn Long-Tail Knowledge](#). 2022b.
5. Alex Mallen, Akari Asai, Victor Zhong, Rajarshi Das, Daniel Khashabi, Hannaneh Hajishirzi. [When Not to Trust Language Models: Investigating Effectiveness of Parametric and Non-Parametric Memories](#). 2022.
6. R. Thomas McCoy, Shunyu Yao, Dan Friedman, Matthew Hardy, Thomas L. Griffiths. [Embers of Autoregression: Understanding Large Language Models Through the Problem They are Trained to Solve](#). 2023.

## Influence Functions

7. Pang Wei Koh, Percy Liang. [Understanding Black-box Predictions via Influence Functions](#). 2017.
8. Samyadeep Basu, Philip Pope, Soheil Feizi. [Influence Functions in Deep Learning are Fragile](#). 2020.
9. Juhan Bae, Nathan Ng, Alston Lo, Marzyeh Ghassemi, Roger Grosse. [If Influence Functions are the Answer, Then What is the Question?](#) 2022.

## Semi-Parametric Language Models

10. Urvashi Khandelwal, Omer Levy, Dan Jurafsky, Luke Zettlemoyer, Mike Lewis. [Generalization Through Memorization: Nearest Neighbor Language Models](#). 2020.
11. Sewon Min, Suchin Gururangan, Eric Wallace, Hannaneh Hajishirzi, Noah A. Smith, Luke Zettlemoyer. [SILO Language Models: Isolating Legal Risk In a Nonparametric Datastore](#)

## Retrieval Augmented Generation

12. Patrick Lewis, Ethan Perez, Aleksandra Piktus, Fabio Petroni, Vladimir Karpukhin, Naman Goyal, Heinrich Küttler, Mike Lewis, Wen-tau Yih, Tim Rocktäschel, Sebastian Riedel, Douwe Kiela. [Retrieval Augmented Generation for Knowledge-Intensive NLP Tasks](#). 2020.
13. Benjamin Cohen-Wang, Harhsay Shah, Kristian Georgiev, Aleksander Madry. [ContextCite: Attributing Model Generation to Context](#). 2024.